# Mathematics 1-Quadratic Equations 

## Topics: Computer engineering <br> Written on March 13, 2024

## 1. Definition:

- A quadratic equation is a second-degree polynomial equation in one variable. It has the form: $\mathrm{ax}^{\wedge} 2+\mathrm{bx}+\mathrm{c}=0$
- Here, $\mathrm{a}, \mathrm{b}$, and c are constants, and x is the variable. a cannot be equal to 0 , otherwise, it wouldn't be a quadratic equation.


## 2. Solutions:

- Quadratic equations typically have two solutions, which can be real or complex numbers. These solutions are called roots or zeroes of the equation.
- The solutions can be found using methods like factoring, completing the square, quadratic formula, or graphical methods.


## 3. Discriminant:

- The discriminant $(\Delta)$ of a quadratic equation is given by: $\Delta=\mathrm{b}^{\wedge} 2-4 \mathrm{ac}$
- The discriminant determines the nature of the roots:
- If $\Delta>0$, the equation has two distinct real roots.
- If $\Delta=0$, the equation has exactly one real root (the roots are repeated).
- If $\Delta<0$, the equation has two complex roots.


## 4. Vertex:

- The vertex of a quadratic function in the form $y=a x^{\wedge} 2+b x+c$ is given by the point (h, k ), where: $\mathrm{h}=-\mathrm{b} / 2 \mathrm{a}$ and $\mathrm{k}=\mathrm{f}(\mathrm{h})=\mathrm{ah} \wedge 2+\mathrm{bh}+\mathrm{c}$


## 5. Graph:

- The graph of a quadratic equation is a parabola. The direction of the parabola (upward or downward) depends on the sign of the leading coefficient a.
- The axis of symmetry of the parabola is a vertical line passing through the vertex.


## 6. Applications:

- Quadratic equations are widely used in various fields, including physics, engineering, economics, and computer science.
- They describe many natural phenomena, such as projectile motion, the shape of satellite dishes, and the pricing of products based on supply and demand.

